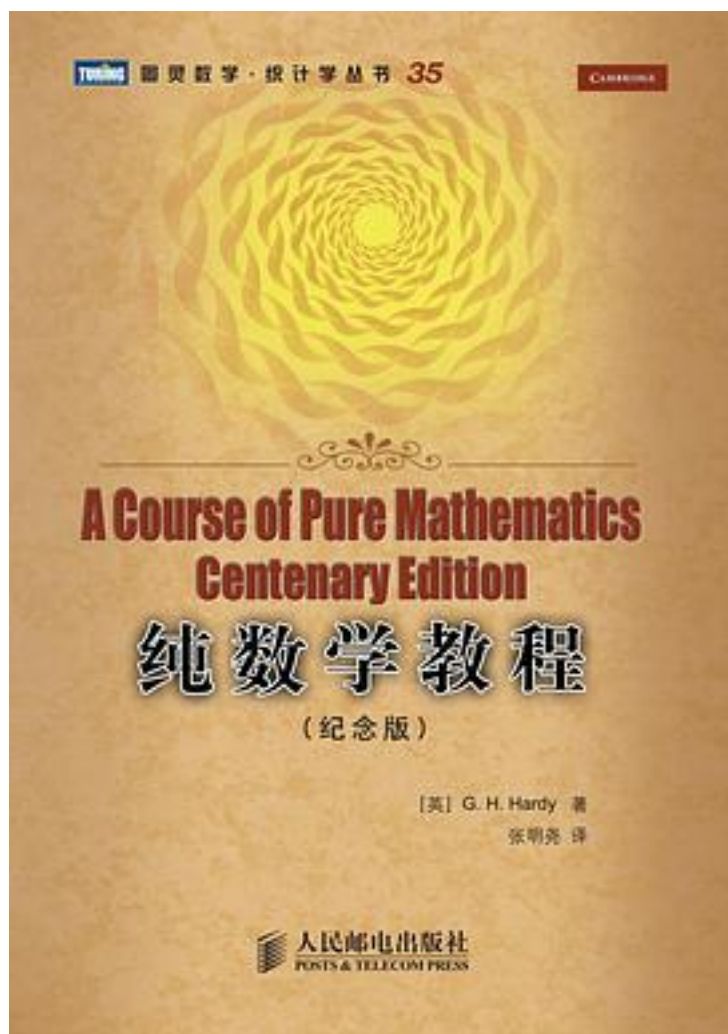


纯数学教程



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自从1908年出版以来，这本书已经成为一部经典之著。一代又一代崭露头角的数学家

正是通过这本书的指引，步入了数学的殿堂。

在本书中，作者怀着对教育工作的无限热忱，以一种严格的纯粹学者的态度，揭示了微积分的基本思想、无穷级数的性质以及包括极限概念在内的其他题材。

作者介绍:

G.
H.Hardy英国数学家(1877—1947)。1896年考入剑桥三一学院，并于1900年在剑桥获得史密斯奖。之后，在英国牛津大学。剑桥大学任教，是20世纪初著名的数学分析家之一。

他的贡献包括数论中的丢番图逼近、堆垒数论、素数分布理论与黎曼函数，调和分析中的三角级数理论。发散级数求和与陶伯定理。不等式、积分变换与积分方程等方面，对分析学的发展有深刻的影响。以他的名字命名的Hp空间(哈代空间)，至今仍是数学研究中十分活跃的领域。

除本书外，他还著有《不等式》、《发散级数》等10多部书籍与300多篇文章。

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评论

《素数之恋》作者John Derbyshire推崇的微积分教材

今天看其实有些陈旧

: O13

哈代书貌似不好找。当年在浙大以两块钱买下这本书。。。现在毕业了却找不到了

很差的一本书

经典 但过时了

epsilon-delta部分也比较细致

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书评

书名是A Course of Pure Mathematics，实际上名不副实，因为书里只讲了基本的分析学原理，没有其他的数学内容（除了那几个附录讲了些别的主题，比如怎么证明代数基本定理）。哈代是个优秀的数学家。在哈代之前，剑桥大学拥有许多杰出的应用数学家，比如Green, Stokes还有Max...

这本书是英国“第一本”分析书

哈代是一位纯粹的数学家。这本书说“我未做任何努力去迎合工科学生，或兴趣主要不在数学的那些学生的需要”
书中讲授的内容编排和国内的书也有很大的不同，可以在学分析时借鉴。
习题都在内容之间穿插着。很多习题都是剑桥考试题

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