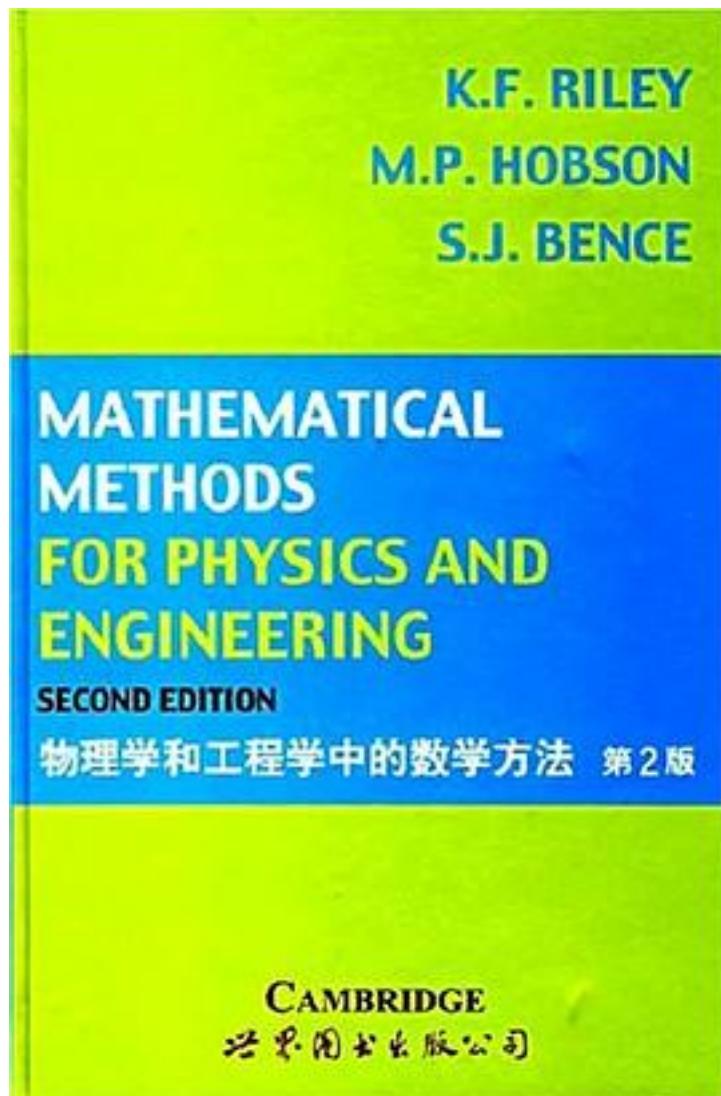


物理学和工程学中的数学方法



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Since the publication of the first edition of this book, both through teaching the material it covers and as a result of receiving helpful comments from colleagues, we have become aware of the desirability of changes in a number of areas. The most important of these is that the mathematical preparation of current senior college and university entrants is now less thorough than it used to be. To match this, we decided to include a preliminary chapter covering areas such as polynomial equations, trigonometric identities, coordinate geometry, partial fractions, binomial expansions, necessary and sufficient condition and proof by induction and contradiction.

作者介绍:

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preface to the first edition

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1.6 properties of binomial coefficients

1.7 some particular methods of proof

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标签

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评论

此书几乎是把整个大学所需的数学集合在一起，而不是传统的数理方法教材。在这一点上，我还是觉得读专门教材更划算一些。

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书评

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