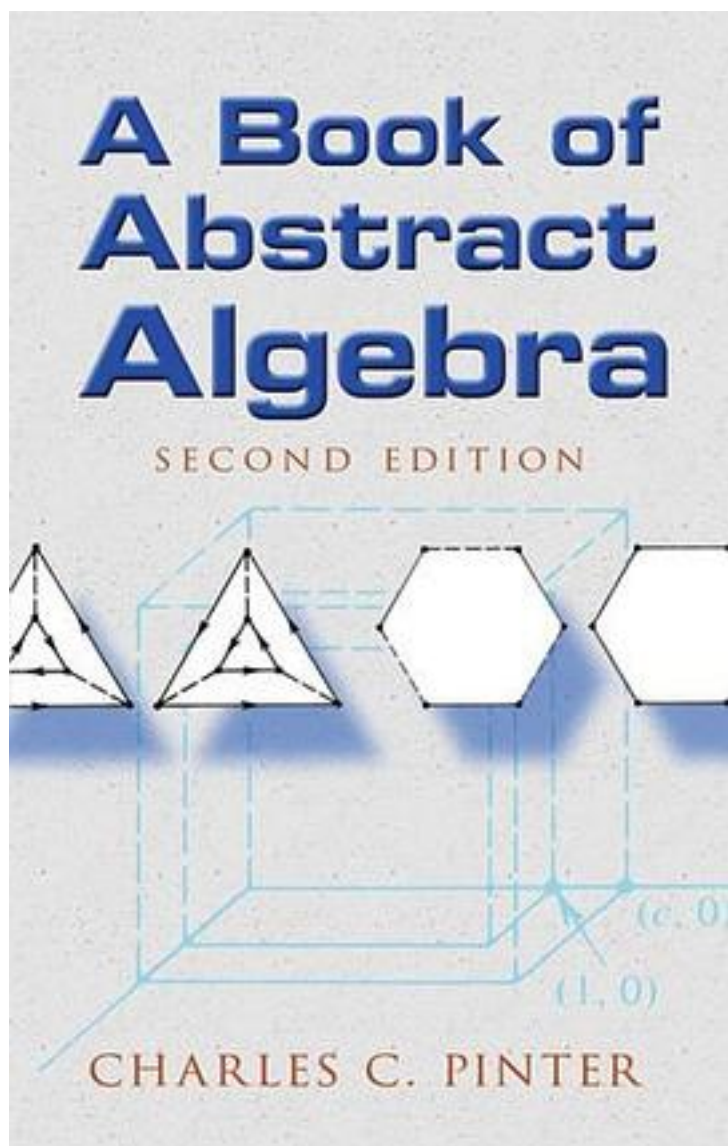


A Book of Abstract Algebra



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Accessible but rigorous, this outstanding text encompasses all of the topics covered by a typical course in elementary abstract algebra. Its easy-to-read treatment offers an intuitive approach, featuring informal discussions followed by thematically arranged exercises. This second edition features additional exercises to improve student familiarity with applications. 1990 edition.

作者介绍:

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标签

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评论

亲测十分简单 读者友好 尽管有些approaches确实挺猥琐的
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